

OKLAHOMA STATE UNIVERSITY  
SCHOOL OF ELECTRICAL AND COMPUTER ENGINEERING



**ECEN 4413/MAE 4053**  
**Automatic Control Systems**  
**Spring 2006**  
**Final Exam**



**Choose any four out of five problems.**  
*Please specify which four listed below to be graded:*

1) \_\_\_\_\_; 2) \_\_\_\_\_; 3) \_\_\_\_\_; 4) \_\_\_\_\_;

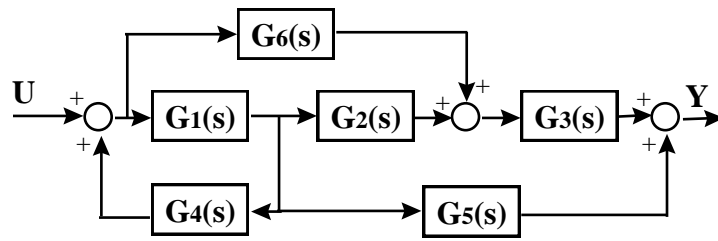
**Name :** \_\_\_\_\_

**Student ID:** \_\_\_\_\_

**E-Mail Address:** \_\_\_\_\_

**Problem 1:**

Using the block diagram reduction technique, find the plant transfer function  $G_p(s)$  in the G-configuration.



**Problem 2:**

The following differential equation represents linear time-invariant system, where  $u(t)$  denotes the input and  $y(t)$  the output,

$$\frac{d^2 y(t)}{dt^2} + \frac{dy(t)}{dt} + 5y(t) = \dot{u}(t) + 2u(t)$$

Find the transfer function  $Y(s)/U(s)$  of the system. In addition, express the system in the state space form of  $\dot{x} = Ax + Bu$ ,  $y = Cx + Du$ . Clearly indicate how the state variables are chosen.

**Problem 3:**

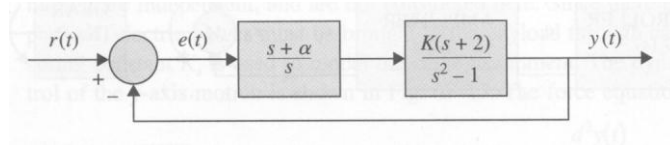
Given a nonlinear system described by

$$\ddot{y} - \dot{y} - e^{a+1}y = \ddot{u} + \dot{u} + 2u,$$

linearize the system about the equilibrium point and show the linearized state space representation in  $\dot{x} = Ax + Bu$ ,  $y = Cx + Du$ .

**Problem 4:**

The block diagram of a control system is shown below. Find the region in the  $K$  vs.  $\alpha$  plane for the system to be stable. (Use  $K$  as the vertical and  $\alpha$  as the horizontal axis.)



**Problem 5:**

Considering the state feedback control system shown below, determine the feedback coefficients ( $k_1$  and  $k_2$ ) so that the poles of the closed-loop control system are located at -5 and -7.

